

# **A Framework for Moving Beyond Computational Reproducibility: Lessons from Three Reproductions of Geographical Analyses of COVID-19.**

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## Abstract

Despite recent calls to make geographical analyses more reproducible, formal attempts to reproduce or replicate published work remain largely absent from the geographic literature. The reproductions of geographic research that do exist typically focus on computational reproducibility - whether results can be recreated using data and code provided by the authors - rather than on evaluating the conclusion and internal validity and evidential value of the original analysis. However, knowing if a study is computationally reproducible is insufficient if the goal of a reproduction is to identify and correct errors in our knowledge. We argue that reproductions of geographic work should focus on assessing whether the findings and claims made in existing empirical studies are well supported by the evidence presented. We present three model reproductions of geographical analyses of COVID-19 that demonstrate how to achieve this goal. Each reproduction is based on a common, open access template and is published as an open access repository, complete with pre-analysis plan, data, code, and final report. We find each study to be partially reproducible, but moving past computational reproducibility, our assessments reveal conceptual and methodological concerns that raise questions about the predictive value and the magnitude of the associations presented in each study. Collectively, these reproductions and our template materials offer a practical framework others can use to reproduce and replicate empirical spatial analyses and ultimately facilitate the identification and correction of errors in the geographic literature.

**Keywords:** Reproducibility, COVID-19, Spatial Regression, GIScience

# 1 Introduction

2 The geographic literature is quickly becoming crowded with calls to make geographical research more re-  
3 producible (see Brunson, 2016; Muenchow, Schäfer, and Krüger, 2019; Yin et al., 2019; Kedron et al.,  
4 2021c; Kedron et al., 2021b; Goodchild et al., 2021; Brunson and Comber, 2021). In principle, repro-  
5 ducible research publicly discloses the evidence base for claims from prior work not only to improve the  
6 transparency of scientific communication, but to also facilitate the independent verification of those claims  
7 (Schmidt, 2009; Nosek, Spies, and Motyl, 2012; Earp and Trafimow, 2015). Reproducibility is therefore  
8 tied to at least two questions about the results and claims of prior work (NASEM, 2019). First, are the data  
9 and methods used in a prior study shared clearly enough to allow for the results to be recreated? Second,  
10 once an attempt to recreate the results of a prior study has been made, do the data, analysis, and results in fact  
11 support the claim(s) made by the study? Research that addresses either question can help make geographic  
12 research more reproducible and facilitate the verification and accumulation of geographic knowledge.

13 To date, geographers have largely focused their efforts on the first of these two questions and have  
14 worked to assess and address whether the data, code, and methods needed to reproduce research are available.  
15 Researchers have catalogued the availability of data and code in subsets of the geographic literature (Konkol,  
16 Kray, and Pfeiffer, 2019; Ostermann and Granell, 2017), identified actions geographers can take to better  
17 share their data and methods (Kedron et al., 2021c; Tullis and Kar, 2021), offered guidelines for how to  
18 do so (Wilson et al., 2021; Hofer et al., 2019; Nüst and Pebesma, 2021), and created infrastructure to host  
19 researcher materials and recreate analyses (Wang, 2016; Yin et al., 2019; Nüst and Hinz, 2019). These  
20 activities set the stage for reproduction studies that assess the claims made in the existing geographic literature  
21 but do not themselves directly check the state of our knowledge.

22 Formal attempts to reproduce published studies and assess whether the claims presented in those studies  
23 are well-supported remain largely absent from the geographic science literature. The few recently pub-  
24 lished reproduction studies that exist in the field focus on assessing whether studies can be computational  
25 reproduced—whether the computational results of a prior study can be recreated using the same data and  
26 code. These studies are similar to traditional manuscript reviews, but additionally attempt to execute avail-  
27 able code, numerically compare the outputs of those attempts to those reported in the manuscript, and report  
28 (and sometimes correct) errors in code compilation or execution. While these studies do attempt to reproduce  
29 prior results, they do not take the additional step of explicitly assessing whether the evidence presented in fact  
30 supports the claims made. Narrowly focusing reproduction attempts on recreating the results and correcting  
31 the coding errors of prior studies reduces reproduction to a form of quality audit that provides limited infor-  
32 mation about the conclusion validity and internal validity of prior work. This approach is understandable,  
33 as the reproducibility crisis across the sciences is often linked to the ubiquitous use of expanding computing  
34 resources to perform complex analyses of complicated problems (see NASEM, 2019; Stodden, Leisch, and  
35 Peng, 2014; Stodden et al., 2016). Unfortunately, ending the evaluation of a study at an assessment of its  
36 computational reproducibility may even hinder scientific progress if others mistake the recreation of results  
37 as an affirmation of questionable decisions that led to those results.

38 We advocate that geographers move beyond checks of computational reproducibility and additionally  
39 begin to develop a body of reproduction studies focused on the assessment of the claims of prior work. To  
40 facilitate this transition, we make three principle contributions in this paper. First, we introduce a model  
41 workflow for conducting reproduction studies aimed at assessing the claims of published research. Second,  
42 to demonstrate the use of our approach and materials, we report the findings of our attempts to reproduce  
43 and assess the claims of three published geographical analyses of COVID-19 in the United States. Third, we  
44 review the reproduction process and use the information gathered during our attempts to identify how we  
45 might systematically use reproduction studies to assess and enhance future geographical research. Through  
46 these contributions, we position geographers to build on recent efforts to make reproducibility more achiev-  
47 able and shift their focus to the evaluation of research through rigorous recreation and reanalysis. Our work

1 therefore reorients the field toward the second question posed by the NASEM, which to this point has been  
2 under-discussed in the geographic literature.

3 The remainder of this paper is organized into six sections. The following section provides background  
4 on reproduction studies in the geographical sciences. We highlight the current focus on computational re-  
5 production and argue for a more comprehensive approach to reproduction in which the reproducing authors  
6 document, catalog, and evaluate research decisions and claims. In the third section, we present our approach  
7 to reproduction in the form of a model workflow and a set of open template materials, and we discuss how to  
8 implement our approach. In the fourth section, we shift to our three reproduction studies. We establish the  
9 need to reproduce studies of COVID-19 and outline our selection of candidate studies. We then describe how  
10 we conducted our three exemplar reproductions in the fifth section. In the sixth section, we present results  
11 from each reproduction study, selected from our published reports and organized to illustrate how repro-  
12 ductions studies can be used to identify and address issues in the conceptualization, measurement, analysis,  
13 and communication of research. Those findings inform a concluding section that outlines how we might  
14 continue to use reproduction and replication to advance geographical analysis.

## 15 **2 The Reproduction of Geographic Research**

16 Numerous geographers have made calls to strengthen geographical analysis by improving the reproducibility  
17 of geographic research and making reproduction studies part of normal disciplinary practice (Brunsdon,  
18 2016; Kedron et al., 2021b; Brunsdon and Comber, 2021; Goodchild et al., 2021; Goodchild and Li, 2021;  
19 Kedron et al., 2021c). In a reproduction study, independent researchers evaluate prior research by attempting  
20 to recreate the results of a study using the data and procedures of the original work (NASEM, 2019). During  
21 a reproduction study, the researchers conducting that study may focus on different goals. It is helpful to  
22 distinguish which of the two questions raised by the NASEM (2019) a researcher wishes to answer. First, if  
23 a reproduction study is focused on simply establishing whether the specific results of the original study can  
24 be recreated, or second, if the reproduction study is focused on whether the data, analysis, and results in fact  
25 support the conclusions and claims drawn from the original study.

26 When narrowly focused on identifying if results can be recreated, a reproduction study acts as a check of  
27 how a study was executed and shared. The NASEM (2019) categorizes this type of reproduction study as an  
28 enriched form of literature review. Simply recreating the result of a study does not establish the validity of  
29 the claims made by the researchers that conducted the original study. It merely guarantees that information  
30 about the data and methods required to assess those claims is shared with sufficient openness and detail for  
31 someone to recreate the results. Such reproductions studies are therefore simply audits of prior research for  
32 the quality of reproducibility. In the era of sophisticated methods and reproducibility crises, such quality  
33 audits may restore some degree of trustworthiness to research, but contribute limited information about the  
34 quality of the research design or validity of the claims made.

35 When a researcher attempts to reproduce a study, they either have access to, or must attempt to iden-  
36 tify, the decisions and materials used to create the prior result. As the reproducing researcher gathers this  
37 information and uses it to recreate the earlier work, they also have the opportunity to evaluate the claims of  
38 the original researchers in light of their decisions, and to evaluate and test each decision against alternative  
39 options (Clemens, 2017; Christensen, Freese, and Miguel, 2019). If the reproducing researcher possesses  
40 the requisite knowledge and chooses to take these opportunities, they may gain information about how the  
41 prior study was conceptualized, designed, and executed, which they can use to make qualified statements  
42 about whether the conclusions reached about relationships in the data are reasonable (conclusion validity),  
43 and whether those relationships may be attributable to other factors (internal validity). Statements about the  
44 conclusion or internal validity of a study must be qualified because any assessment remains contingent upon  
45 numerous additional factors such as the design of the original study and the expertise of the reproducing re-

1 searchers. While reproductions never provide conclusive evidence for or against a finding, they can provide  
2 insight into whether a study has a flawed research design or if errors were made during its execution (Nichols  
3 et al., 2021; Earp and Trafimow, 2015). Once identified, studies can be redesigned and errors can be cor-  
4 rected. In this way, reproduction studies help us progressively improve our understanding of phenomena by  
5 reducing the number of errors we make and lessening our uncertainty.

6 A flurry of recent activity has begun to create an environment to support reproduction studies in the the  
7 geographical sciences. Workshops and conference sessions (see Nüst et al., 2018; SPARC, 2019; Kmoch,  
8 Nüst, and Uuemma, 2020) have started to create a research community around the subject, while review  
9 articles (Brunsdon, 2016; Kedron et al., 2021c) and a special issue in the *Annals of the American Asso-*  
10 *ciation of Geographers* have raised awareness. Several publications have also laid crucial foundations by  
11 connecting reproduction to the discipline's traditions (Wainwright, 2020; Wolf et al., 2021) methodologi-  
12 cal approaches (Brunsdon and Singleton, 2015; Singleton, Spielman, and Brunsdon, 2016; Kedron et al.,  
13 2021b), educational priorities (Muenchow, Schäfer, and Krüger, 2019; Kedron et al., 2021d), and theoret-  
14 ical debates (Goodchild and Li, 2021; Sui and Kedron, 2021; Kedron and Holler, 2022a). Accompanying  
15 development of computational and institutional infrastructure (see Wang, 2016; Nüst and Hinz, 2019; Nüst  
16 and Pebesma, 2021; Konkol, Nüst, and Goulier, 2020; Wilson et al., 2021) has reduced the barriers to con-  
17 ducting reproductions. Despite these developments, few formal reproductions have been published in the  
18 geographic literature.

19 The reproductions that do exist in the geographic literature typically focus on establishing whether it  
20 is possible to recreate the outcomes of a prior study by cataloging study components that can affect re-  
21 producibility, or verifying specific computational results. For example, Ostermann and Granell (2017) use a  
22 literature review of volunteered geographic information research publications to assess computational repro-  
23 ducibility based on availability of original data, metadata, source code, or pseudocode. Researchers taking  
24 part in an ongoing reproducible research initiative of the Association of Geographic Information Laborato-  
25 ries in Europe have reviewed the computational reproducibility of 31 research paper results submitted to that  
26 association's annual conference for the past three years (Nüst et al., 2020; Nüst et al., 2021; Nüst et al., 2022)  
27 and 75 papers from the GIScience conference series (Ostermann et al., 2021). In addition to assessing the  
28 availability of data, methods (code), and results, the researchers also attempted to independently re-execute  
29 the coded analyses of submitted papers and share their findings in the form of short reproducibility reports.  
30 Konkol, Kray, and Pfeiffer (2019) similarly attempted computational reproductions of the coded analyses of  
31 41 open-access research papers applying spatial statistical methods and found most difficult to computationally  
32 reproduce. While this research usefully summarizes technical barriers to computational reproducibility,  
33 all of these authors limit their discussion to coding errors and differences in figures and maps. Similarly,  
34 while these authors helpfully use their findings to derive guidelines for publishing computationally repro-  
35 ducible research, their central focus is on determining whether an independent researcher can re-execute a  
36 study's analytical code and create identical outputs.

37 In contrast, if the primary goal of a reproduction study is to assess whether the data, analysis, and results  
38 of a study in fact support the claims made by a researcher, then it is insufficient to stop a reproduction  
39 attempt when the code is found to fail or succeed at exactly recreating the original results and figures. In the  
40 geographical sciences, it is critical for a researcher seeking to evaluate a work by attempting to reproduce it  
41 to attend to threats to validity involving geographic space (Schmitt, 1978). Reproductions lend themselves  
42 to evaluations of the conclusion or internal validity of a study. If a study has a flawed research design, or  
43 is poorly executed, it may nonetheless be computationally reproducible. Even if a study is well-designed  
44 and properly executed, reproducing the results without critically reflecting on the design and execution of  
45 the study will do little to advance our knowledge. To understand whether a result is credible or reliable, a  
46 researcher conducting a reproduction study must also examine how the original researchers conceptualized,  
47 designed, and implemented their study (Kedron et al., 2021b). If research findings depend on decisions that  
48 are not justified, then the findings themselves are not justified (Christensen, Freese, and Miguel, 2019).

1 When an independent researcher makes an argument that there is a better way to analyze the original data  
2 than was reported in a study, reproduction can be a platform for introducing procedural differences that we  
3 think may affect the result of the original study. By introducing those changes we may begin to determine  
4 whether the approach adopted by the original researchers was somehow inadequate or erroneous. Davies  
5 (1968) provides an early example of this approach to reproduction in geography. In a paper examining  
6 the predictions of central place theory, Davies reanalyzes the data of two studies using slightly different  
7 techniques to draw conclusions about the validity of the original analysis and offer possible extensions for  
8 future work. A few reproductions by Kedron et al. (2021a) and Kedron et al. (2022a) have brought this  
9 approach into the present, but formal, published reproductions and replications that systematically examine  
10 the entire research process remain rare in the geographic literature.

### 11 **3 A Practical Approach to the Reproduction of Geographic Research**

12 The present dearth of reproductions evaluating the entire research process is likely due, at least in part, to the  
13 current absence of a model approach that researchers can use to guide their own reproduction attempts. Here  
14 we introduce such an approach, and a workflow and template materials to facilitate its implementation by  
15 others. Building on prior workflow models of the computational reproduction process, we developed a three-  
16 stage workflow (Fig. 1) to guide the reproduction of geographic research. Our workflow model presents a  
17 high-level organization of key tasks common across reproduction attempts. Almost every component within  
18 the model could be further expanded into a significant sub-model and customized for different sub-disciplines  
19 in geography. However, we restrict our presentation here to the higher-level because our goal is to instigate  
20 a shift in how we pursue reproduction across a variety of research areas. Below, we outline the Planning,  
21 Implementation, and Evaluation steps of our approach.

22 To facilitate adoption, we have paired our model with a template repository designed to help organize  
23 the reproduction process. The repository contains document templates and suggestions on how to use and  
24 modify the repository structure. Our template repository is available online as a Git repository under a BSD  
25 3Clause License through (Kedron and Holler, Mar. 2022b). We used these materials to conduct the repro-  
26 ductions presented in this paper.

27

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#### 28 **3.1 Planning**

29 Before beginning any data analysis, researchers attempting a reproduction should first carefully deconstruct  
30 the design and implementation of the prior analysis and create a workflow model for their own analyses.  
31 It is essential that researchers clearly articulate the aspects of the prior study they intend to reproduce. For  
32 example, in the case of hypotheses-driven research the reproducing research should communicate which  
33 research questions and hypotheses will be the focus of their reproduction and how they intend to gather data,  
34 execute their analyses, and compare their results. While this step may appear trivial, many studies do not  
35 formally state their hypotheses and provide only a partial description of their analytical plans. Researchers  
36 also often test a large number of hypotheses during the course of their study but highlight only an handful in  
37 their results. This situation leaves the reproducing researcher to choose which hypotheses to recreate and to  
38 explain why some hypotheses may have been chosen over others.

39 We suggest that researchers formally record and present their reproduction workflow as part of a pre-  
40 analysis plan that details the data collection, processing, and analysis they intend to undertake as part of  
41 their reproduction attempt. The workflow should be based on the most complete and precise understanding  
42 of procedures that is possible based upon reading the original publication and- ideally- on reading supple-  
43 mentary materials including data and code. In lieu of sufficient procedural detail, the plan should include

1 the reproducing researchers' best approximation of the procedures for data processing and analysis. This  
2 pre-analysis plan should also include the criteria they intend to use to compare their results to those of the  
3 original study. Ideally, researchers will publicly register this plan before they begin their reproduction at-  
4 tempts. Pre-analysis plans can be shared via platforms like GitHub, or more formally registered through  
5 services like the Open Science Framework <sup>1</sup>.

6 In the exemplar reproductions presented below, our student collaborators created the initial workflow  
7 models and drafted pre-analysis plans, which the lead authors reviewed and commented upon. We found  
8 iterative revisions of the plans to be vital for identifying issues of ambiguity, uncertainty, and error in the  
9 original research design. We suggest researchers catalog such issues as they arise during the reproduction  
10 attempt.

## 11 **3.2 Implementation**

12 Once pre-analysis planning is completed, most reproduction attempts will move on to data collection, prepa-  
13 ration, and analysis. A common practical barrier is whether or not the data used in the original analysis is  
14 accessible, or whether the protocol and procedures used to gather that data is available. In some instances,  
15 if data are not available with the publication they can be accessed from an original source (e.g., US Census).

16 Data are almost always processed prior to analysis, and ideally the reproduction will use original code  
17 for data processing, analysis, and visualizing results. Whether the reproduction study can reuse code from  
18 the original study or needs to write new code, any changes or deviations from the original procedural plan  
19 should be documented. Whether available with the study or accessed from a common original source, data  
20 are almost always processed prior to analysis.

21 Pre-analysis plans are designed to be dynamic documents and communication tools for tracking unantic-  
22 ipated changes that occur throughout the reproduction process as researchers work to resolve the conceptual  
23 and practical challenges that arise during the reproduction process. As the pre-analysis plans are created and  
24 implemented as reproduction procedures or code, any ambiguities the reproducing researchers must resolve  
25 should be cataloged as issues that will be later categorized and evaluated following the Kedron et al. (2021b)  
26 framework. The decisions of reproducing researchers should also be included as amendments to the pre-  
27 analysis plan.

28 To move beyond computational reproducibility, researchers can introduce differences into their reanal-  
29 yses to test the sensitivity of the original analysis to alternative conceptualizations or research designs. As  
30 these variations are introduced they should be tracked in the issues catalog along with the reasoning support-  
31 ing each change. These differences can be categorized in the same way as researcher decisions, which will  
32 bring their evaluation into a common framework.

## 33 **3.3 Evaluation**

34 We suggest that researchers compare their reproduction results to those of the original study as they are  
35 created. If discrepancies arise early in the analysis (e.g., differences in descriptive statistics), we suggest  
36 revising the procedures and documenting the unplanned deviations from the original workflow in the pre-  
37 analysis plan before proceeding to subsequent analyses.

38 There is no universally agreed upon set of criteria to assess whether the results of an original study have  
39 been reproduced, and much of the literature related to the subject focuses on the more complicated question  
40 of replication (see Verhagen and Wagenmakers, 2014; OSC, 2015; Simonsohn, 2015; Lakens, 2017). Prior  
41 reproductions of geographic researcher have based their evaluation on either an exact match of numerical  
42 results, or the similarity of figures and maps. We suggest at minimum evaluating the direction, magnitude,  
43 and levels of uncertainty associated with both sets of results in any comparison. Differences between results

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<sup>1</sup>See Christensen, Freese, and Miguel (2019) and Olken (2015) for a discussion of the pros and cons of pre-registration

1 will often motivate the introduction of further variations in research design and analysis. When those are  
2 pursued they should be cataloged and categorized like other issues and tracked as deviations from the original  
3 reproduction plan.

4 Critically, we view the documentation and comparison of the results of a reproduction attempt as only  
5 one part of the evaluation process. To use a reproduction to evaluate the claims made by the authors of the  
6 original study, we argue that the reproducing authors should also evaluate the complete set of decisions made  
7 during the creation of that result in light of our existing understanding of the of the phenomena under study.  
8 This task is where the cataloging and categorizing of issues and decisions that we advocate for throughout  
9 the reproduction process plays a role. That catalog can now be used to contextualize decisions made by the  
10 original and reproducing authors and the evidence of the reproduction results within the existing literature,  
11 providing a foundation for evaluating the research claims.

## 12 **4 Empirical Context, and the Selection of Studies for Reproduction**

### 13 **4.1 Empirical Context**

14 To demonstrate our approach and how it differs from computationally focused reproductions, we attempted  
15 to reproduce geographical analyses of COVID-19. The COVID-19 pandemic has highlighted the need to  
16 make reproductions and replications a standard part of the geographic research process. The rate of research  
17 publication during the pandemic has led to concerns over the quality of peer review and the rate of retractions  
18 (Yeo-Teh and Tang, 2020). Well into the COVID-19 pandemic, researchers continue to produce studies  
19 intended to advance our understanding of the spatial patterns of this disease (e.g., Sun et al., 2020; Sugg et al.,  
20 2021; Chakraborty, 2021) and the spatial processes that may be responsible for the spread of the SAR-CoV-2  
21 virus (e.g., Andersen et al., 2021; Lee and Ramírez, 2022). Moreover, many of these geographical analyses  
22 have been undertaken by researchers with primary research interests and expertise outside of geography,  
23 and published at an accelerated pace due to the urgency and scale of the pandemic. Medical professionals,  
24 government officials, and policymakers are using this stream of research to revise their response to the  
25 pandemic. To ensure those groups have access to the best possible research so they can make the best  
26 possible decisions, we must know more than the results of recent geographical analyses of COVID-19. We  
27 must also know how reliable and credible those results are, because understanding the credibility of research  
28 allows us to appropriately weight findings when making decisions about pandemic response. Understanding  
29 the validity of these studies is also important because they are already becoming the foundation for future  
30 research.

31 Recognizing this situation, several authors (see Gustot, 2020; Sumner et al., 2020; Collins and Alexan-  
32 der, 2021) have emphasized how important it is that COVID-19 research be reproducible and have begun  
33 to catalog the availability of code and data within in the COVID-19 literature. Geographers have produced  
34 similar catalogs of geographical analyses of COVID-19, but have limited their reviews to listing and cat-  
35 egorizing the literature by topical focus and methodological approach (see Ahasan et al., 2020; Agbehadji  
36 et al., 2020; Franch-Pardo et al., 2020; Franch-Pardo et al., 2021). To our knowledge, only one formal re-  
37 production of geographical analyses of COVID-19 is presently available in the published literature (Kedron  
38 et al., 2021a). Conducting reproductions of COVID-19 research will allow us to assess the internal validity  
39 of selected studies and draw lessons about how we might use reproduction as a widely adopted means of  
40 geographic research assessment.



## 4.2 Selection of candidate studies for reproduction

### 4.2.1 Study selection

To identify candidate studies for reproduction, we conducted an electronic search for peer-reviewed spatial analyses of COVID-19 published in English language journals between January 01, 2020 and March 15, 2021. The central objective of our search was to identify spatial analyses that demonstrate how reproduction can be used to critically appraise published work. To enhance the impact of our work, we sought to identify studies that relied on the most commonly used sources of COVID-19 data and were based on spatial methods frequently used in spatial epidemiology. These criteria allow our reproductions to inform our development of a practical framework and model for others to follow when reproducing empirical spatial analysis.

Candidate studies were identified by searching Elsevier's Scopus database using the search query:

("COVID-19" OR "SarS-CoV-2" OR "2019-nCoV" OR "2019 coronavirus" OR "2019 novel coronavirus" OR "novel coronavirus") AND ("GIS" OR "Spatial Analysis" OR "Geospatial Analysis" OR "ArcGIS" OR "Geographic Information System" OR "Geographic Mapping")

We designed this query to mirror the search criteria of Ahasan et al. (2020)'s review of geographical analyses of COVID-19. We also independently searched the Google Scholar database using the same search terms to identify additional studies that match the objective of this review. The Scopus search was run February 09, 2021 and the Google Scholar search was conducted February 18, 2021. A limited updated literature search was performed between March 15, 2021 and March 30, 2021. These searches yielded 540 unique articles. We then collected the abstracts and full texts for each of these articles.

Article abstracts were selected for further review if they were: 1) published in an English language journal, 2) peer-reviewed, 3) topically focused on the COVID-19 pandemic, and 4) geographically focused on the United States. These criteria narrowed the selection of articles to 60. Articles were then reviewed for a fifth criteria: application of spatial statistical methods common in spatial epidemiology and compatible with graduate student training in spatial statistics (e.g., spatial regression and pattern analysis). This review narrowed our list to 15 candidate articles that were further reviewed for their 1) complete publication details, 2) study objectives, 3) data sources, 4) data and code availability, and 5) spatial methodology.

Based on this information, we selected three articles – Mollalo, Vahedi, and Rivera (2020), Saffary et al. (2020), and Vijayan et al. (2020). These articles used spatial statistical methods common in both spatial epidemiology and the broader geographic literature and appeared feasible to reproduce. These articles also provided a level of detail about the research process typical of the broader literature - information about data sources, hypotheses, and methodology was provided. As such these articles provided us with the opportunity to demonstrate the use of reproduction as a form of reanalysis and critique that extends beyond the matching of computational outputs.

### 4.2.2 Characteristics of the studies selected for reproduction

The three studies selected for reproduction use spatial regression techniques and local spatial statistics to make associational inferences about COVID-19 (Table 2). Mollalo, Vahedi, and Rivera (2020) fit a series of spatial regression models to evaluate variation in county-level COVID-19 incidence using a set of socio-economic and demographic characteristics as predictor variables. The authors present five regression models including an ordinary least squares (OLS) model, spatial lag model (SLM), spatial error model (SEM), geographically weighted regression (GWR), and a multiscale GWR (MGWR). Neither the data nor the code used for the original analysis was made available by the authors. Saffary et al. (2020) use bivariate Moran's I to examine whether socio-demographics and healthcare resources are correlated in space with COVID-19 cases and deaths across the contiguous United States. The authors do share the county-scale data used in

1 their analyses. Vijayan et al. (2020) examine whether spatial patterns existed in SARS-CoV-2 age-adjusted  
2 testing rates, age-adjusted diagnosis rates, and crude positivity rates in Los Angeles County (LAC), and use  
3 a spatial regression model to explore associations between COVID-19 crude positivity rates and a series of  
4 predictor variables. Although not publicly available, we were able to obtain the original study data after con-  
5 tacting the authors. The analysis code was not made available, nor was information about the computational  
6 environment used.

7

« Insert Table 1 About Here »

## 8 5 Implementation of the Reproduction Attempts

9 We followed the three-stage process of planning, implementation, and evaluation outlined by our model  
10 approach (Fig. 1) for each of the three reproductions we attempted. The entire reproduction process for  
11 each study is documented in a research compendium that includes our reproduction plans, reports, data, and  
12 code. Each compendium is available online as a Git repository under a BSD 3-Clause License to allow other  
13 researchers to examine our approach and use our work as a model for future reproductions. The details of  
14 each reproduction can be accessed through **removed for anonymous peer-review**.

15 During the planning stage of each reproduction attempt, we focused on developing a model workflow  
16 and pre-analysis plan. We used an iterative process to create the reproduction workflow. Each team member  
17 developed their own model workflow, which they then presented to the other authors. We then collectively  
18 identified the chain of researcher decisions and points of uncertainty that needed to be addressed, as we  
19 developed a single common workflow model. Those workflows then became the foundation of our pre-  
20 analysis plans, which also identified the key hypotheses we sought to re-test and any deviations from the  
21 original analyses we anticipated due to a lack of information provided in the original study.

22 We used the authors' provided materials to the greatest extent possible as we implemented our reproduc-  
23 tion attempts. When available, we used publicly available data provided by authors. When not available, we  
24 acquired the public data described in the article or contacted the corresponding author to request inaccessible  
25 data. We attempted to use the processing environment described in the original study but also translated the  
26 workflow into R code version 4.0.4 (R Core Team, 2021). Whenever possible, we followed the procedures  
27 described in the original article or provided in the form of code. When we encountered missing or uncertain  
28 information with regard to data sources or procedures, we attempted the reproduction using alternative data  
29 sources and procedural decisions.

30 Following our model approach, our evaluation of each reproduction attempt consisted of two assess-  
31 ments: (1) an assessment of result similarity and computational reproducibility, and (2) an evaluation of the  
32 execution and claims of the original study. Mirroring existing reproductions of geographic research that fo-  
33 cus on verification and recreating results with the same data and code, we used the simple criteria of whether  
34 the results of the reproduction and original analysis were numerically or graphically identical to assess re-  
35 producibility. We applied this criteria to analyses that have analytical solutions (e.g., OLS regression or  
36 local statistics evaluated using the normality assumption). However, several of the analyses we attempted  
37 to reproduce relied on conditional permutation of the data to estimate parameters (e.g., direct/indirect effect  
38 estimation) or made statistical inferences (e.g., local statistical inferences). In these instances, we relaxed  
39 the criteria of identical reproduction and instead focused our evaluation on the comparison of parameter es-  
40 timates, related uncertainty estimates, and statistical significance. ( $p$ -values)<sup>2</sup>. These criteria mirror those

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<sup>2</sup>Gelman and Stern (2006) present the challenge of comparing statistical significance across studies and caution against basing conclusions on changes in significance alone. We incorporated this thinking into our analyses but retained comparisons of significance levels, because as reproductions our work uses the same data and methods, which should lead to the same or very similar significance levels.

1 presented by the NASEM (2019) and those used by OSC (2015). We were able to partially verify the original  
2 findings of each of the three studies by computationally reproducing a portion of the original results, albeit  
3 not without challenges (Section 6.1).

4 Our deep reading, attempts to recreate the workflows of the original studies, and efforts to achieve com-  
5 putational reproduction revealed numerous questions and concerns about the the design and implementation  
6 of each study. Those questions motivated our further investigation of the internal validity through a reanaly-  
7 sis of each study. Moving beyond an assessment of computational reproducibility, we evaluated each study  
8 using the framework presented by Kedron et al. (2021b) and linked points of concern that arose during each  
9 reproduction attempt to different stages of the research cycle. We also compared those issues across the  
10 studies to identify common points of strength or weakness (section 6.2).

11 After completing the reproduction attempts, we created reproduction reports by updating the original  
12 pre-analysis plan to include a record of any unplanned deviations from the posted plan, the results of the  
13 reproduction including comparison to the original study, and a discussion of the results. All team members  
14 reviewed each report, and after revisions, final reports were posted within each reproduction compendium.

## 15 **6 Lessons from the Three Reproductions**

### 16 **6.1 Computational Reproductions**

17 We were able to partially reproduce the analyses and results of each of the three studies we investigated  
18 (Table 2). The extent to which we were able to reproduce the results of each study was directly related to the  
19 availability of original data and the detail of the procedural description provided, as none of the authors shared  
20 their original code. We were able to create exact reproductions of nearly all the tables and maps presented  
21 by Saffary et al. (2020) in part because these authors provided their data file. Conversely, Mollalo, Vahedi,  
22 and Rivera (2020) did not provide their data and offered limited descriptions of their data sources. This gap  
23 hindered our reproduction attempt and produced the least consistent results. We were similarly unable to  
24 reproduce the results of Vijayan et al. (2020) on our initial attempt, because we could not reconstruct the  
25 hexagonal tessellation, or access the identical neighborhood-level COVID data. Once the authors provided  
26 these data upon request, we were able to create an exact reproduction of their descriptive statistics and obtain  
27 consistent spatial regression estimates.

28 To achieve a partial reproduction of each study, we had to make unplanned deviations from our initial  
29 analytical plans. For example, while Saffary et al. (2020) published their analytic data file, that file did not  
30 include one of the key independent variables, requiring us to gather this missing variable from public sources.  
31 While we were able to collect the necessary data, some locations in the file had missing values. The authors  
32 provided no information as to how to handle those missing values, which we ultimately determined were  
33 simply omitted from analysis. While we were able to obtain consistent regression estimates when reproduc-  
34 ing Vijayan et al. (2020), we had to adjust our original plans when reproducing the authors' LISA analyses.  
35 Our reproductions of the authors' LISA analysis found low-high and high-low clusters that were either not  
36 identified or not reported by the original authors. If these clusters were purposefully omitted, this decision  
37 represents a cartographic form of observed selective inference. We similarly found inconsistencies in how  
38 Mollalo, Vahedi, and Rivera (2020) presented the variables in their paper and how they appear to have been  
39 processed in their analyses. For instance, the authors did not mention standardizing their variables prior to  
40 analysis, yet the magnitude of the reported coefficients suggest that they had been standardized. The authors  
41 also reported using the percentage of nurse practitioners as one of their independent variables, but their de-  
42 scription of the variable calculation suggests that the count of nurse practitioners was used.

43

« Insert Table 2 About Here »

## 6.2 Beyond Computational Reproductions

Our attempts to reproduce the computational result of the three selected studies uncovered procedural, statistical, and inferential questions that raised concerns about the internal validity and credibility of each study. Following our model approach (see section 3), we cataloged those concerns, linked them to the stages of the research cycle (Table 3), and introduced procedural changes that allowed us to test the affect alternative decisions had on each analysis. To demonstrate the value of this form of reproduction, we discuss the issues we encountered in relation to phases of the research process.

« Insert Table 3 About Here »

### 6.2.1 Conceptualization and Design

Many of the issues we encountered when designing our reproduction attempts and interpreting their results stemmed from the conceptualization and design of the original studies. We found four overarching issues of concern. First, the authors of our target studies did not address the epistemic uncertainties potentially impacting their analyses. For example, in each study the primary response variable was the count of COVID-19 cases or deaths early in the pandemic. In principle, we could have known these counts. However, in practice there was limited and geographically variable testing capacity during the study periods, and asymptomatic cases often went undetected. These factors likely contributed to a spatially varying undercount of disease prevalence. Acknowledging this systematic uncertainty in case and death counts (Halpern et al., 2021) is important because geographic variation in count reliability can impact parameter estimation. To be clear, we would not expect the authors to resolve these issues with the data available. However, understanding and explaining how uncertain critical measurements are is fundamental to placing inferences and claims in a proper context. This issue constrains the ability of our reproductions to validate these studies. While reproducing this work allowed us to identify this concern, our results and inferences are similarly impacted by this issue.

Second, we believe these studies would benefit from deeper consideration of how the spatial and temporal supports of their data impact analysis. Two of the studies use counties as their spatial support, while the third constructs a hexagonal grid. This selection seems to be largely a matter of data availability and convenience that is mismatched with our knowledge of the transmission dynamics of COVID-19 (Wali and Frank, 2021). For example, while Vijayan et al. (2020) use a hexagonal grid as their spatial support, variable construction within that grid ignored variation in the geography of the administrative units of the original data. Moreover, the Census data used as predictors of COVID-19 incidence was collected before the pandemic raising questions about the spatial support of each study. While we expect some degree of temporal consistency in the socio-demographic profiles of these units, the pandemic also created migration patterns (Coven, Gupta, and Yao, 2020; Haslag and Weagley, 2021) that may make measures from several years before the pandemic a poor match to the actual populations present in those location during the pandemic. Addressing these mismatches is difficult given data availability and the rapidity of the pandemic, but acknowledging and discussing the potential impact of measurement issues would help readers better understand the implications and reliability of each study. Moreover, recent studies in different geographic contexts (González-Leonardo et al., 2022; Rowe et al., 2022) point to alternative measures of population migration that could be now used to reassess these issues.

Third, our reproduction attempts led us to question how the original authors incorporated the current understanding of the epidemiology of COVID-19 into their operationalization of spatial relationships and their selections of the spatial scale of their analyses. Two of the three studies we reproduced sought to identify ecological predictors of COVID-19, and were conducted using counties as the spatial support for all analyses. However, epidemiological research suggests that counties are not a meaningful unit of analysis for

1 COVID-19 transmission, which happens at a much finer spatial scale (Wali and Frank, 2021). Even when  
2 counties are used as proxies to measure ecological relationships, it is critical to adjust for other factors that  
3 would influence transmission within and between counties, such as population density or the presence of a  
4 large urban center. These factors were not included in the original analyses, which may have led to erroneous  
5 inferences. For example, it is not clear that these studies provide evidence of a predictive link between racial  
6 minority status and COVID-19 case counts when adjusting for urban-rural differences that were not included  
7 in the analyses. How the authors treated spatial scale also appears to have led to instances of the atomistic  
8 fallacy, which we discuss in 6.2.3.

9 Fourth, when interpreting the results of our reproduction attempts, we found it difficult to identify why  
10 the authors included some ecological factors in their models but excluded others. We were unable to assess  
11 how reliable identified associations were when potentially important confounding factors were omitted from  
12 the analyses. Without understanding why the authors believed a factor would affect aggregated COVID-19  
13 case or death counts at a particular scale, we could not assess how the patterns presented provided information  
14 about the processes that might be responsible for them.

## 15 **6.2.2 Measurement and Processing**

16 We invested substantial labor in reconstructing the original data and data processing procedures for the three  
17 reproduction studies. In the process, we discovered concerns related to construct validity and variable con-  
18 struction. For example, the article by Saffary et al. (2020) contains ambiguities and inconsistencies with  
19 regards to the handling of missing data and data standardization. As one example, the authors provide no  
20 information about their handling of missing county level data for their primary care physician variable. We  
21 investigated three alternative procedures to address this issue - filtering, zero imputation, and mean imputa-  
22 tion. Our findings suggest the authors simply omitted missing values. In other instances, Saffary et al. (2020)  
23 chose not to standardize their variables by population size. For example, the authors analyzed the raw count  
24 of intensive care unit beds in each county. However, the strong positive correlation between the number of  
25 such beds and county population likely makes this essentially a measure of county population.

26 In other instances, although Vijayan et al. (2020) indicate the standardization of variables prior to spatial  
27 regression modeling, they are not clear as to whether this standardization was applied to both the response  
28 and predictor variables. Moreover, the authors provide limited information about the specification of their  
29 spatial regressions, which makes it difficult to interpret their results. Nonetheless, the authors report and  
30 discuss their coefficient estimates without referencing the fact that these results are based on standardized  
31 variables and that the model intercept was omitted from their analysis.

32 Our reproduction attempts also uncovered questions about how the original authors created the spatial  
33 support for their analyses. This concern is best illustrated by Vijayan et al. (2020) who based their statistical  
34 analyses on a 10km hexagonal grid that they superimposed onto Los Angeles County, CA. The authors  
35 did not (1) present a clear justification as to why this grid was an appropriate unit of analysis, (2) provide  
36 the information needed to reconstruct the grid, or (3) include a discussion of how their data aggregation  
37 procedures might impact their analyses. We ultimately determined that the authors aggregated data originally  
38 linked to different areal units (e.g., Census tracts, municipalities) to their hexagonal grid based on the overlap  
39 between that grid and the centroids of the areal units of the data. This approach ignores the proportion of  
40 geographic overlap between the hexagonal grid and the source data and could lead to non-representative  
41 measurements. For example, the age-adjusted response variables used in these analyses are problematic.  
42 Given that the age-adjustment was not based on the population within the hexagonal units but the mix of  
43 areas whose centroids fell within a given hexagon, these response variables are no longer accurately age-  
44 adjusted. Selecting a single unit of analysis and aggregating data in this way introduces unknown amounts  
45 of measurement error into any subsequent analysis and creates the possibility for inferential errors.

### 6.2.3 Analysis and Inference

Our reproduction attempts allowed us to draw several cautionary lessons about the implementation and interpretation of spatial statistical tests of COVID 19. First, the authors of all three studies did not clearly present the complete discrete set of hypotheses they tested prior to their analyses. Each study made statements about expected associations between COVID-19 incidence and some key independent variables, but did not formalize these hypotheses. In some cases, the authors also tested other unstated hypotheses or tested the stated hypotheses multiple times. Without formal hypothesis statements, these studies are best viewed as exploratory analyses of possible spatial associations between aggregated measures.

Second, our reproductions highlight the need to carefully consider, and explain in text, the reasoning supporting the conceptualization of scale and spatial relationships implemented during spatial statistical tests. In these three studies, the reasoning behind the implementation of the statistical tests seems to be subject to the atomistic fallacy. In each study, the authors root their variable selection and model specification decisions in knowledge and reasoning about the individual-level dynamics of COVID-19 transmission. However, a geographic area is used as the spatial support for analysis in each study and the variables used in each statistical test are aggregated to those units. These choices implicitly scale the individual-level reasoning for variable selection to the group level at these geographic scales. This scaling may be fallacious. For example, Saffary et al. (2020)'s use of the Bivariate Moran's I to measure associations across space extends their assumptions about individual-level associations and disease dynamics to the group-level and inter-county-scale. It is not clear, for example, that the evidence and reasoning supporting the belief that an individual person of color might be at a higher risk of contracting COVID would extend to all people of color in a county, or to all people of color in counties surrounding a county with COVID cases. We suggest that this type of epidemiological study that is based on aggregate social data should be interpreted with caution as exploratory and should be supported by further individual-level or multi-scale research.

Additionally, We have no information about how sensitive each study may be to the modifiable areal unit problem because each study only reported a single spatial support and spatial extent. It may well be the case that studying these relationships at a different spatial scale would change these results. As one example, Vijayan et al. (2020) use of a single 10km hexagonal grid as the spatial support for their analysis provided. Selection of another grid size may produce different estimated associations between predictor variables and COVID-19 rates. The results of this analysis may be particularly sensitive to variation across spatial supports given that the centroid overlap-based aggregation of data will produce different levels of measurement error for each hexagonal grid size. We suggest that this form of uncertainty can be better understood by testing result sensitivity to alternative spatial supports and utilizing alternative methods of spatial reaggregation based on overlap of tract areas or residential buildings.

Third, our reproductions suggest spatial statistical analyses of COVID-19 may be subject to model specification and interpretation problems. For example, Mollalo, Vahedi, and Rivera (2020) considered 34 variables for inclusion in their regression analyses, but relied on a stepwise forward selection procedure to reduce this set to a final total of 4 variables. This data-driven approach to variable selection positions their final model as a general, exploratory analysis. With only four variables in the final model it is likely that the model does not properly control for important confounding factors that may influence both the predictor and response variables, and thus, the model coefficients are likely to be biased.

These issues are compounded by the authors reliance on fit statistics to guide model selection and to measure explanatory power. Based solely on the higher R-squared and lower AICc of their MGWR model, the authors recommend the continued monitoring of these factors to understand spread of the disease. However, this recommendation ignores both the poor model fit of the OLS specification and the maps of the local R-squared from both the GWR and MGWR models which show large numbers of counties with negative R-squared values. Combined, these indicators suggest model underspecification while the substantial difference in the goodness of fit between the local and global models is indicative of overfitting in the local

1 models. We propose a need to balance data-driven exploratory analyses with more deductive theory-based  
2 approaches to spatial epidemiological modelling with registered pre-analysis plans in order to develop the-  
3 orized mechanisms with inferential power.

4 Similarly, our reproduction of Saffary et al. (2020) revealed inconsistencies in the implementation and  
5 interpretation of the Bi-variate Local Moran's I statistic. When interpreting this statistic, the authors dis-  
6 cuss COVID-19 rates as a measure of correlation. However, the statistic was implemented using each focal  
7 county's rate of COVID-19 incidence and the spatial lag of adjacent counties' health and demographic com-  
8 positions. Contrary to the interpretations presented, this implementation suggests that the COVID-19 rates in  
9 a county are the product of variable concentrations in surrounding counties. For example, COVID-19 rates  
10 in an urban county may be influenced by the rates of minority residents in surrounding counties exclusive of  
11 the urban minority rate.

12 Fourth, two of the reproductions we attempted revealed that geographical analyses of COVID-19 may  
13 suffer from the problem of uncorrected multiple hypothesis testing. Saffary et al. (2020) search for spatial  
14 clustering provides the clearest example of this issue. In their study, the authors executed thousands of local  
15 univariate and bivariate tests, but included no adjustment for the number of tests in their main manuscript.  
16 As reported, the results are an example of observed selective inference, which occurs when researchers  
17 implement many statistical tests, fail to account for the effects of multiple testing, and then emphasize only a  
18 subset of their results. Making appropriate adjustments for the large amount of multiple testing done during  
19 this analysis is key to making reliable inferences. Using a  $p=0.05$  significance threshold, we would expect  
20 156 'significant' results in a set of 3,105 tests even when no spatial pattern exists. Curiously, Saffary et al.  
21 did include Bonferroni and False Discovery Rate adjustments for multiple testing as a supplement to their  
22 analysis. After applying these adjustments nearly all of the spatial patterns highlighted in the manuscript  
23 disappear. While we were able to reproduce the authors' FDR-adjusted results, our attempt to reproduce the  
24 Bonferroni-adjusted results failed.

#### 25 **6.2.4 Communication**

26 Our reproduction results reinforce the importance of clearly tracking and communicating the provenance  
27 of research before, during, and after a geographical analysis. Many of the problems we encountered when  
28 reproducing these studies could have been avoided had the authors documented and shared information  
29 about the sources, quality, and uncertainty of their data; the decisions and justifications for their analytical  
30 decisions; and the foundations of their conclusions. However, this lack of transparency indirectly led us to  
31 more carefully deconstruct each study, which in turn led us to a deeper understanding of how the authors  
32 designed and executed their research. That process of reanalysis led us to the results presented in the prior  
33 sections and reinforces the value of reproduction as a tool to check the internal validity and credibility of  
34 research. Indeed, many of the problems we identified were not apparent when reading the publications, and  
35 were further obscured through the lack of data, code, and sufficiently detailed procedural description.

36 An additional communication problem we uncovered through our reproductions is the potential pres-  
37 ence of selective inference in these geographical analyses of COVID-19. Selective inference occurs when  
38 statistical inference is focused on a finding only after observing the data (Benjamini, Heller, and Yekutieli,  
39 2009). While we could not directly observe selective inference in these studies, our reproductions show the  
40 many possible avenues through which unobserved selections could occur. For example, in each study the  
41 authors selected a queens contiguity matrix at the county/hexagon scale to represent the spatial relationships  
42 underlying patterns of association with COVID-19. While a reasonable starting point, statistical results are  
43 sensitive to weights selection, and there is no reason to believe this form of contiguity was the only form  
44 tested or the form that appropriately captures the dynamics of the pandemic. Similarly, we demonstrate  
45 above how our reanalyses explored alternative missing data procedures, spatial data supports, and model  
46 specification decisions. The potential for selective inference is also exacerbated by the absence of a clear

1 and complete set of research hypotheses in each study.

2 As published, we cannot know whether selective inferences occurred during these studies, and have no  
3 evidence to suggest the authors intentionally or unintentionally made any selective inferences. However, the  
4 important point is that while we do not know what the authors did, we do have clear evidence that it is very  
5 easy to make unintentional selective inferences in any geographical analysis. To provide evidence that se-  
6 lection did not occur, the complete provenance of the research needs to be recorded and shared. This sharing  
7 should include any sensitivity analyses or specification check the authors preformed as they focus inference  
8 on some models rather than others. Ideally, authors would also pre-register or share their hypotheses and  
9 analytical plans before they observe their data, thus creating a need to justify any deviations from those plans.  
10 Conducting these type of sensitivity analyses and communicating their outcomes frames research decisions  
11 and lends credibility to claims.

## 12 **7 Conclusion**

13 In this paper, we present a model workflow and corresponding materials to help geographic researchers move  
14 beyond using reproduction to simply answer whether the results of a study can be recreated to assessing  
15 whether the data, analysis, and results presented in a study in fact support the claim(s) made by the study  
16 authors. We demonstrate how reproduction studies can act as the foundation for testing alternative research  
17 designs, problem conceptualizations, and analytical pathways, which can lead to improvements in the quality  
18 of geographic research and knowledge production in the discipline. Over the course of this paper, we make  
19 three principle contributions.

20 First, we introduce a model workflow for conducting reproduction studies aimed at assessing the claims  
21 of published research. The conceptual foundation of our approach is Kedron et al. (2021b)'s representa-  
22 tion of the research process as a series of decisions researchers make in the face of uncertainty about the  
23 phenomenon under study. We adopt the authors' four part segmentation of the research process, and their  
24 discussion of some of the challenges particular to reproducing geographical analyses, as a means of tracking  
25 and categorizing decisions made by both the original authors and the researchers attempting to reproduce  
26 their work. In doing so, our approach provides a means of linking the existing literature on challenges and  
27 uncertainties in geographical analyses to aspects of the reproduction process. This approach matches an un-  
28 derstanding of research as a continuous process aimed at refining degrees of confidence in our understanding  
29 of phenomena, rather than establishing complete certainty

30 Second, To demonstrate the use of our approach and materials, we report the findings of our attempts to  
31 reproduce and assess the claims of three published geographical analyses of COVID-19 in the United States.  
32 We were able to partially reproduce each study, and the reproduction process led us to identify a number of  
33 conceptual and methodological concerns that raise questions about the predictive value and the magnitude  
34 of the associations presented in each study. Overall, while already highly cited, we believe the studies we  
35 reproduced and reanalyzed are best viewed as exploratory analyses of spatial patterns of COVID-19 early in  
36 the pandemic. In our view, they provide limited reliable evidence of meaningful associations of substantial  
37 magnitude.

38 In each reproduction study, we go beyond reviewing the availability of data and methods and executing  
39 code. Rather, we attempt to recreate all aspects of the procedures of each study regardless of an absence  
40 of, or errors in, data an code. By retracing each study's procedure, we scrutinize every detail of the work,  
41 including details and decisions not communicated in the published manuscript. We highlight questions about  
42 the spatial reasoning used when designing these studies and problems in the application of spatial statistical  
43 techniques used regularly in the geographic literature. As we encounter shortcomings in the research de-  
44 sign and discrepancies between the manuscript, the procedures, and the reported results, we reanalyze the  
45 study and correct errors. All identified errors and uncertainties in each study are presented and discussed



1 in reports. Each of the three reproduction studies is published with open source licensing as a reproducible  
2 research compendium composed of data, code, pre-analysis plans and detailed reports of our results (Ke-  
3 dron et al., [Apr. 2022c](#), [Apr. 2022d](#), [Apr. 2022b](#)). We thereby improve the computational reproducibility  
4 of these published studies, provide an enriched assessment of their claims, and facilitate any future research  
5 attempting to replicate or extend these studies.

6 Third, we review the reproduction process and use the information gathered during our attempts to iden-  
7 tify how we might systematically use reproduction studies to assess and enhance future geographical re-  
8 search. We identify a series of such threats to conclusion and internal validity involving geographic space  
9 present in the three studies we attempt to reproduce and connect those threats to decision points in the re-  
10 search process. The concerns highlighted in this paper can serve as a guide for others seeking to implement  
11 original research with these techniques in a principled manner. We similarly believe our work can be incor-  
12 porated into coursework when training future geographic analysts, as these analyses were conducted under  
13 the supervision of the lead authors in collaboration with graduate students early in their respective programs.  
14 To our knowledge, this paper is one of the first attempts to push reproduction attempts beyond computation  
15 in the geographical sciences.

16 Despite the concerns revealed by our reproductions, these papers all passed through peer-review and, in  
17 some cases, are garnering significant positions in the literature. As of September 7, 2022, Mollalo, Vahedi,  
18 and Rivera (2020) has received 300 citations on Scopus and 472 citations on Google Scholar. Our work  
19 therefore raises questions about the peer-review process, while demonstrating the value incorporating repro-  
20 ductions into that process might bring. We believe that had reviewers reproduced these studies or had access  
21 to fully reproducible research compendia complete with data and code, they would have found at least some  
22 of the issues we raise. We hope that further revisions would have addressed some of our identified concerns.  
23 However, simply re-executing the code and data used in these studies would not have identified many of the  
24 issues raised in this paper.

25 The discussion and practice of reproducibility in geography should not be limited to matters of sharing  
26 research artifacts and re-computing results. This insight has implications that extend beyond the reproduc-  
27 tion of a single study to the institutional changes we might pursue to improve the creation and accumulation  
28 of geographic knowledge. For one, our findings support a case for geographic journals considering not just  
29 requiring the submission of research materials but also incentivizing comprehensive reproduction studies.  
30 For example, editors could commission reproduction studies of selected articles, pair publications of repro-  
31 ductions and original author response, or create recurrent special issues of reproductions or replications in  
32 their given field. These institutional changes are necessary to identify, communicate, and improve recurrent  
33 issues with geographic analyses in geography and adjacent disciplines.

34 We might similarly incorporate comprehensive reproduction studies into our graduate coursework. Con-  
35 ducting rigorous reproduction is a time consuming endeavour that is currently not incentivized by academic  
36 review process. As such it seems likely that many academics do not conduct formal reproduction, or if  
37 they do conduct them do not pursue the publication of those results, creating the present shortage. We have  
38 demonstrated that graduate students can conduct high-quality reproductions using our practical framework to  
39 structure their approach. Although we did not formally document their experiences, we found graduate stu-  
40 dents interested to engage in the reproduction studies as they provided an opportunity to both learn techniques  
41 and contribute formally to the geographic literature. To this end, folding reproductions into coursework may  
42 produce the dual benefit of introducing more reproductions into the literature while preparing the next gen-  
43 eration of geographic researchers to work in a reproducible manner. Our hope is that this work will start a  
44 culture of reproduction and replication in geography, and the open sharing of any such efforts.

## 1 **CRedit Author Statement**

2 **Kedron** led study conceptualization, methodology, writing; and supervision and administration of reproduc-  
3 tions. **Bardin** performed reproduction attempts and contributed substantially to reproduction review and all  
4 writing tasks. She also led data curation and software development. **Holler** contributed to methodology de-  
5 velopment, writing - review and editing. **Gilman, Grady, Seeley, X. Wang, W. Yang** undertook the initial  
6 reproductions.

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9 took independent reviews of our three reproduction attempts and corresponding repositories as part of their  
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11 Fuller, and Lev VanZanderberg who participated in our initial reproduction attempts.

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Table 1: Characteristics of the geographical analyses of COVID-19 selected for reproduction

	Mollalo et al. (2020)	Saffary et al. (2020)	Vijayan et al. (2020)
Data Available	Yes	No	No
Code Available	No	No	No
Processing Environment	Not specified	Not specified	Not specified
Spatial Extent	USA	USA	LA County
Spatial Support	County	County	10km Hexagons
Temporal Extent	Jan-Apr 2020	Feb-May 2020	Feb-June 2020
Hypothesis Tests	1000s	1000s	1000s
Methods	SEM, SLM, GWR, MGWR	Moran's I, Bivariate Moran's I	Moran's I, SLM

Table 2: Computational reproducibility of the select geographical analyses of COVID-19

	Mollalo et al. (2020)	Saffary et al. (2020)	Vijayan et al. (2020)
Descriptive Statistics	Not specified	Fully	Fully
Direction of Regression Coefficients	Fully	Fully	Partially
Magnitude of Regression Coefficients	Partially	Fully	Fully
Statistical Significance	Fully	Fully	Partially
Maps	Partially	Partially	Partially



Table 3: Points of concern identified during replication attempts

	Point of Concern	Mollalo	Saffary	Vijayan
Conceptualization and Design	Consideration of epistemic uncertainty	X	X	X
	Consideration of scale	X	X	X
	Justification of variable selection	X		X
Measurement and Processing	Details of data processing	X	X	X
	Description of missing data procedures		X	X
Analysis and Inference	Presentation of research hypotheses	X	X	X
	Atomistic fallacy and MAUP	X	X	X
	Model specification and test execution	X	X	X
	Adjustment for multiple hypothesis testing		X	
Communication	Lack of provenance information	X	X	X
	Selective inference	X	X	X

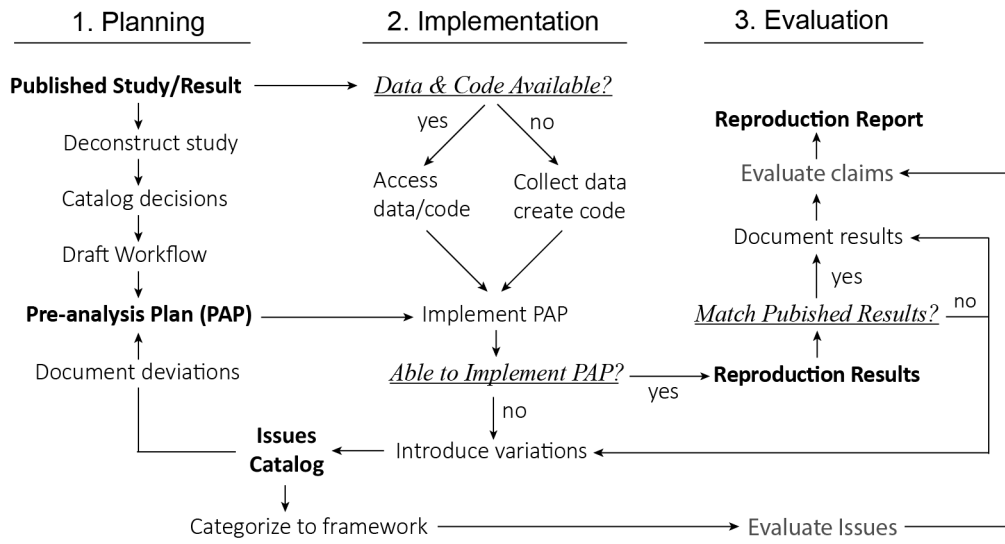


Figure 1: Three stage approach to reproduction

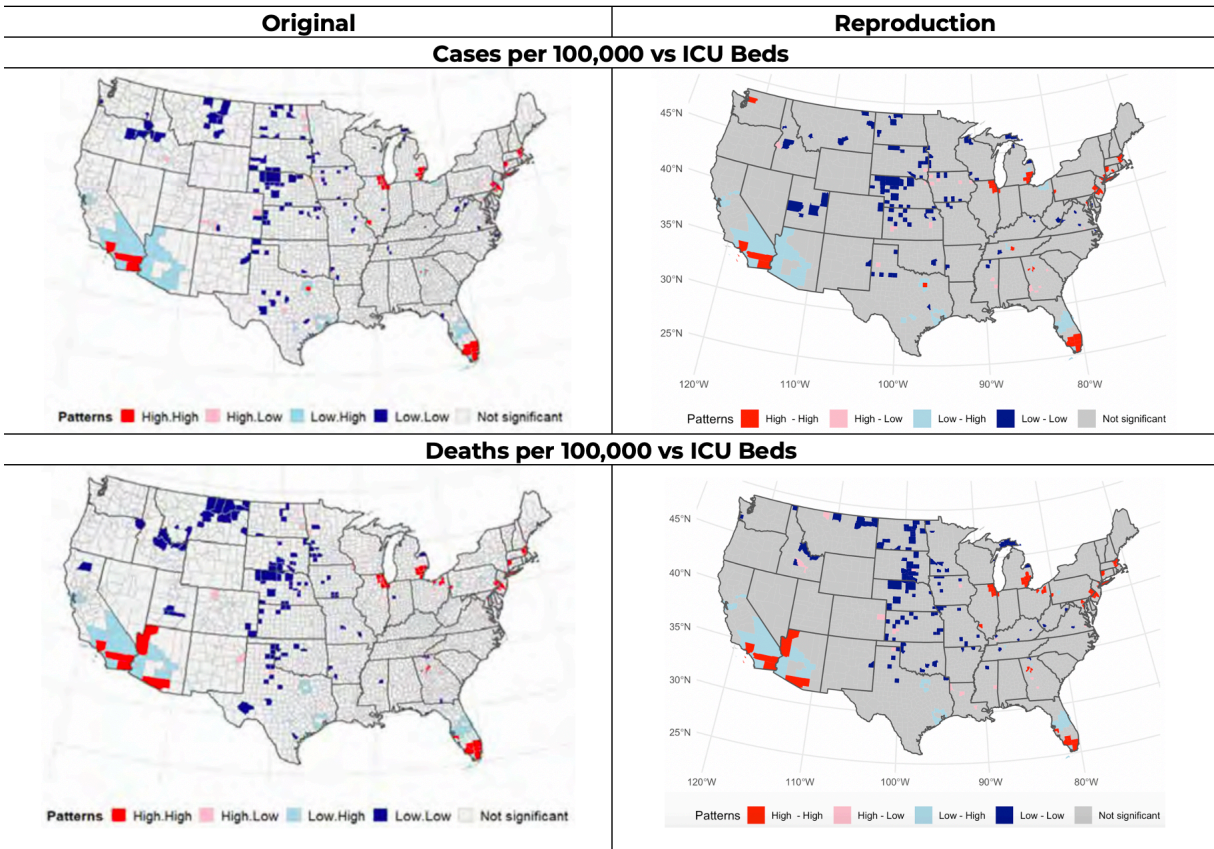


Figure 2: Results from bivariate local Moran's I analysis of number of intensive care unit beds and rate of COVID-19 cases (top) and rate of COVID-19 deaths (bottom) from Saffary et al. (left) and reproduction analysis (right). High-high clusters are denoted in red, high-low clusters are denoted in pink, low-high clusters are denoted in light blue, low-low clusters are denoted in dark blue, and non-significant clusters are denoted in grey.

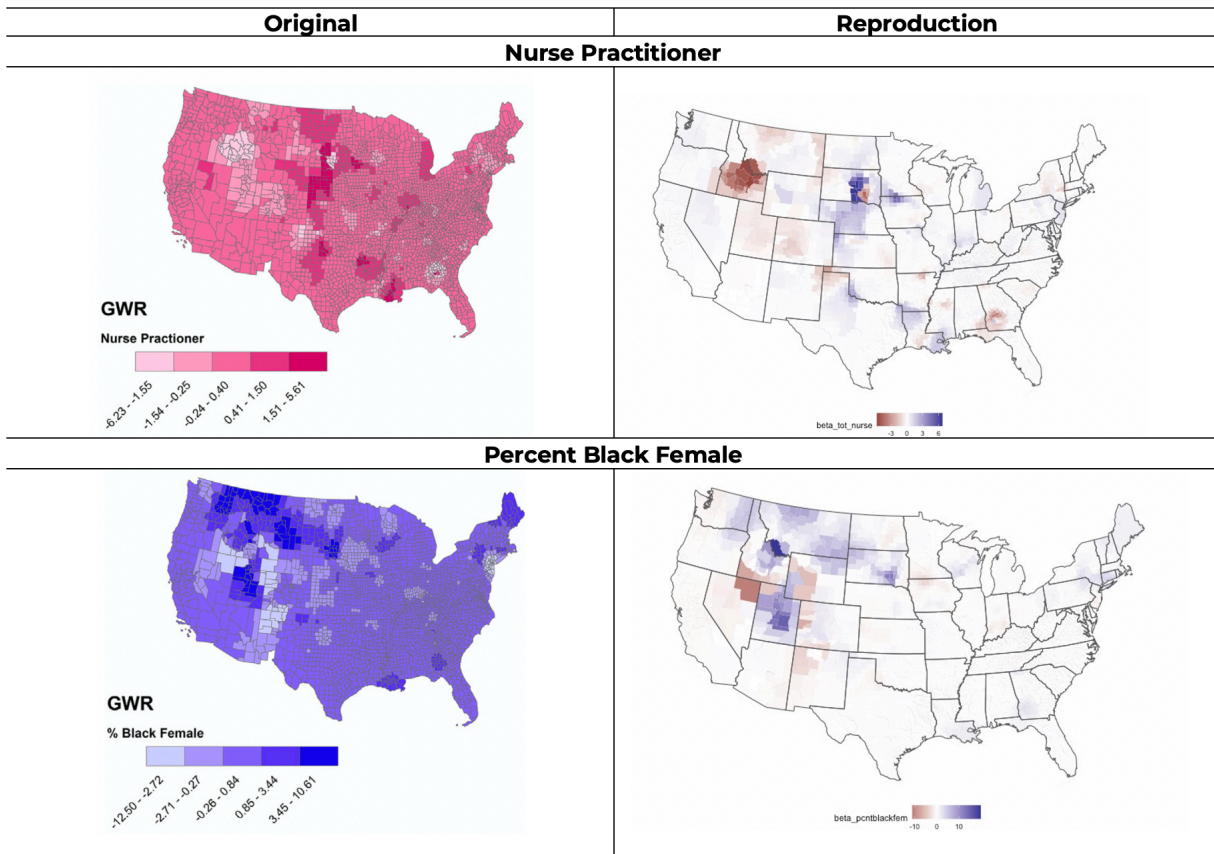


Figure 3: Parameter estimates from Geographically Weighted Regression analysis for the number of nurse practitioners (top) and percent Black females (bottom) from Mollalo et al. (left) and reproduction analysis (right).

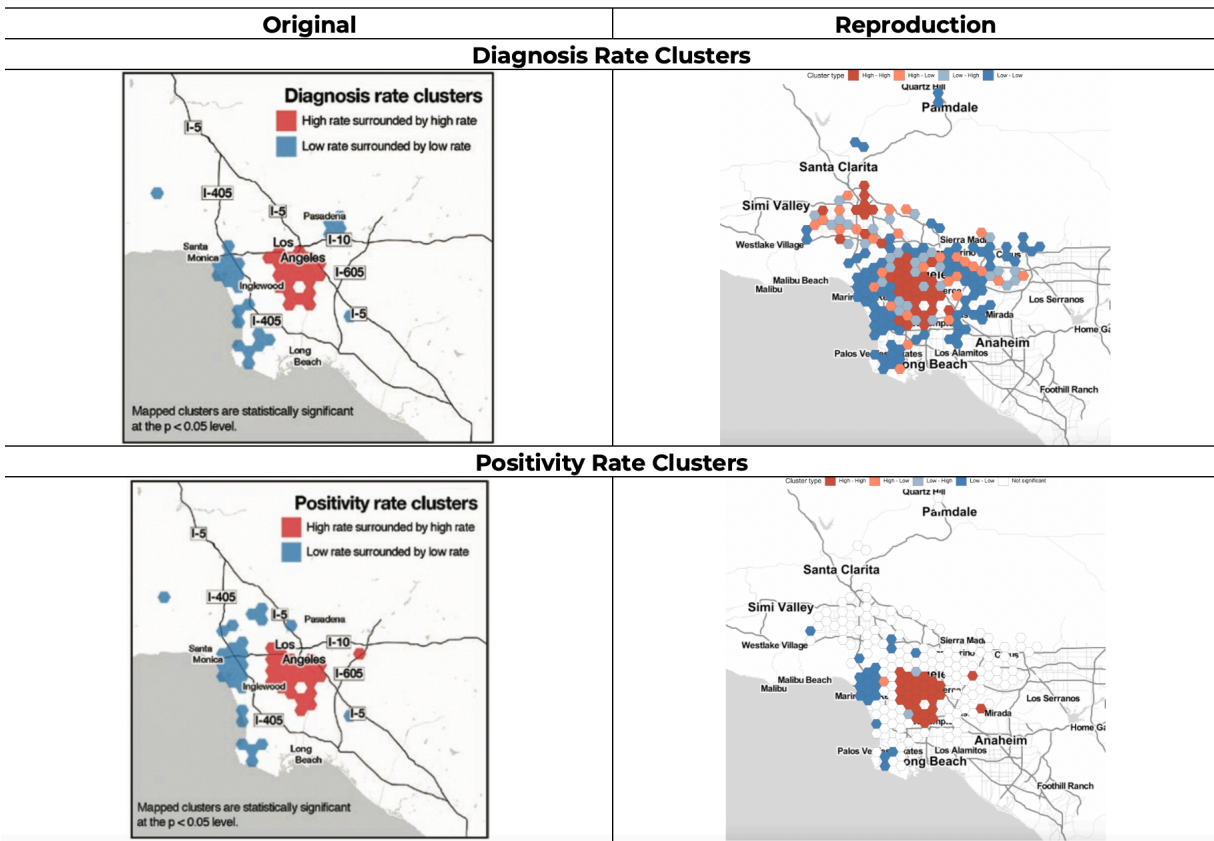


Figure 4: Results from LISA analysis of COVID-19 diagnosis rates (top) and positivity rates (bottom) from Vijayan et al. (left) and reproduction analysis (right). High-high clusters are denoted in red, low-low clusters are denoted in blue, non-significant clusters denoted in white.